




Modulation Nonlinearity and Mitigation Technique in Multiband Radio-over-Fiber Systems

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Outline



- **Introduction**
- **Experimental setup and theoretical analysis**
- **Modulation nonlinearity**
 - Intra-band I/Q cross-modulation
 - 16QAM
 - Inter-band cross-modulation
 - OOK+OOK
 - Both intra- and inter-band cross-modulation
 - 16QAM+16QAM
- **Nonlinearity mitigation: pre-compensation**
 - Intra-band
 - Inter-band

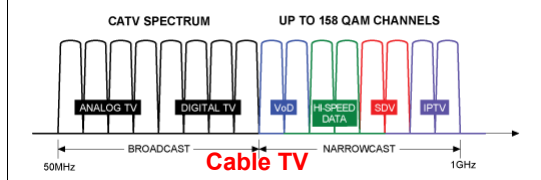
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Examples of Multiband RoF Systems

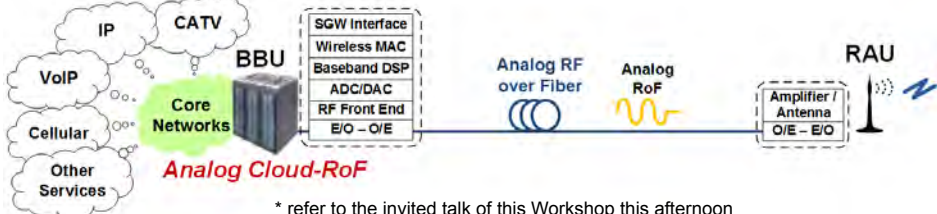


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(a) Cable TV System using HFC Access Technology




(b) Multiband Cloud Radio Access Networks (C-RAN)



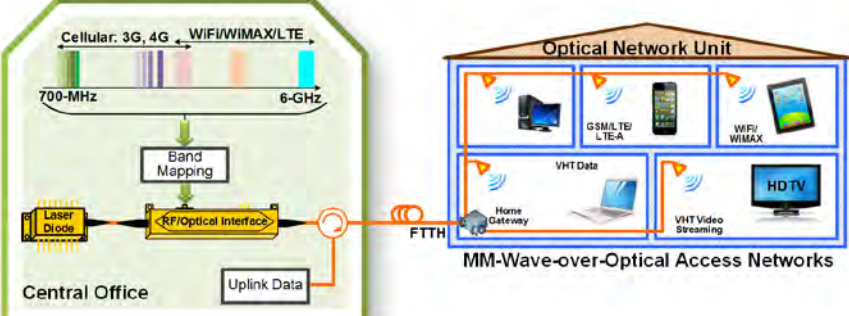
* refer to the invited talk of this Workshop this afternoon

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Indoor Multiband Radio-over-Fiber Systems



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Indoor MM-wave Access Systems

- Pros/cons of multiband analog RoF
 - ☺ Subcarrier multiplexing (SCM) to carry multi-service to multi-users
 - ☺ Capable of direct up-converting legacy wireless services to millimeter wave (mm-wave)
 - ☺ Transparent, compatible and convergent with existing wireless infrastructure
 - ☹ Modulation nonlinearity between multiple bands
 - ☹ Especially for applications with large number of channels, e.g., CATV, mobile backhaul

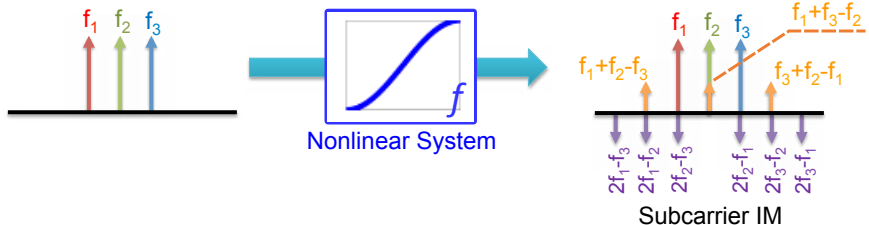
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Introduction



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- Modulation nonlinearity
 - Frequency domain: subcarrier intermodulation (IM) to generate unwanted frequency components
 - Has been extensively investigated
 - Frequency dependent
 - High-order harmonics ($2f$, $3f$, ...)
 - Sum/difference frequencies:
 - Composite triple beat (CTB, $f_1 \pm f_2 \pm f_3$)
 - Two-tone third-order intermodulation (IM3, $2f_1 \pm f_2$)



Subcarrier IM

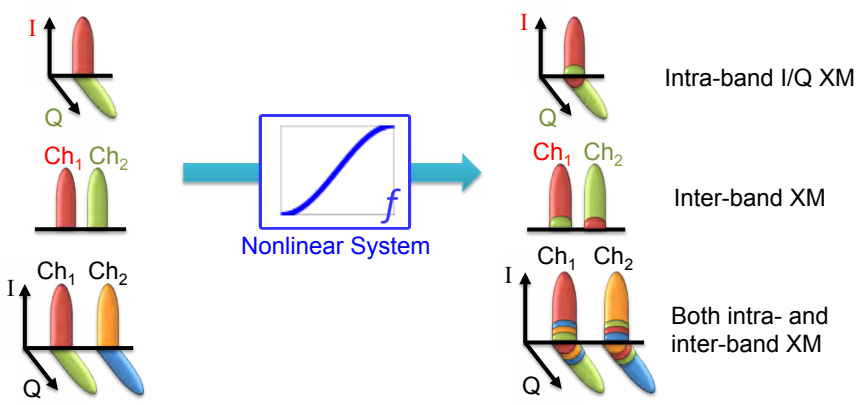
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Introduction



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- Modulation nonlinearity
 - Time domain: data pattern cross-modulation (XM) between different channels
 - Not reported in the field so far
 - Pattern dependent
 - Intra-band: between I/Q channels of a vector signal (e.g. QAM)
 - Inter-band: between two or more data channels at different carrier frequencies



Nonlinear System

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Outline

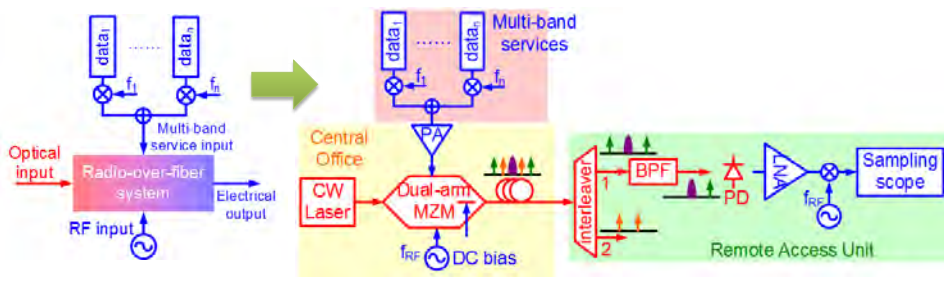


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 - Intra-band
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Experimental Setup




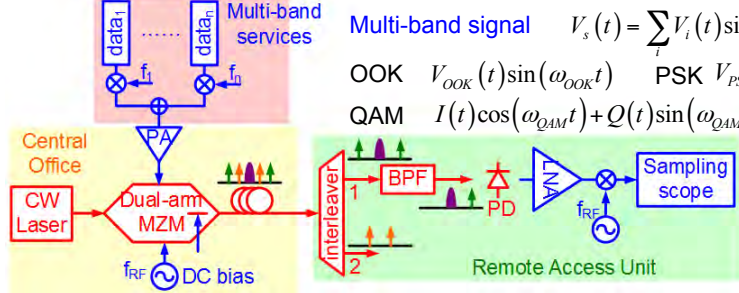


- Dual-arm MZM
 - Upper-arm: multi-band data modulated onto optical central carrier
 - Lower-arm: driven by pure RF to generate multiple sidebands
- Interleaver
 - Separate odd/even sidebands
 - 0th and $\pm 2^{\text{nd}}$ sidebands beat in PD to up-convert data to RF band
 - Pure $\pm 1^{\text{st}}$ RF sidebands are reserved for uplink

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Experimental Setup





Multi-band signal $V_s(t) = \sum_i V_i(t) \sin(\omega_i t + \varphi_i)$

OOK $V_{OOK}(t) \sin(\omega_{OOK} t)$ PSK $V_{PSK} \sin[\omega_{PSK} t + \varphi(t)]$

QAM $I(t) \cos(\omega_{QAM} t) + Q(t) \sin(\omega_{QAM} t)$

Transfer function $T = \frac{1}{2} \left(e^{j\phi_{DC}} e^{j\frac{\pi V_{RF}(t)}{V_\pi}} + e^{j\frac{\pi V_s(t)}{V_\pi}} \right)$

After beating in PD $I_{ph} \propto \cos(2\omega_{RF} t) \left[DC\ const. + \sin\left(\frac{\pi V_s(t)}{V_\pi}\right) \right]$


For best linearity set DC bias

$$\phi_{DC} = \frac{\pi V_{DC}}{V_\pi} = \frac{\pi}{2}, \quad V_{DC} = \frac{V_\pi}{2}$$

- Nonlinearity comes from the **sinusoidal transfer function** of the O/E interface of the optical modulator
- Not only for dual-arm MZM, but also apply to other modulators (IM, PM)

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Theoretical Analysis Results




Bands	Scalar / Vector	Format	Signal $V_s(t)$	Cfr.	Modulation index	Output	Intra-band I/Q XM	Inter-band XM	Distortion	Constellation / Eye diagram
Single-band	Vector	QAM	$I(t)\cos(\omega_c t) + Q(t)\sin(\omega_c t)$	I	$m_1(t) = \frac{\pi I(t)}{V_\pi}$	$J_0(m_1)J_0(m_2) + J_2(m_2)...$	Yes	N/A	Constellation compression	
		PSK	$V_s \sin[\omega_c t + \varphi_s(t)]$	PSK	$m_1 = \frac{\pi V_s}{V_\pi} = const.$	$J_0(m_1) \sin[\omega_c t + \varphi_s(t)]$	No	N/A	No	
		OOK	$V_1(t)\sin(\omega_1 t) + V_2(t)\sin(\omega_2 t)$	OOK	$m_1(t) = \frac{\pi V_1(t)}{V_\pi}$ $m_2(t) = \frac{\pi V_2(t)}{V_\pi}$	$J_0(m_1)J_0(m_2)$	N/A	Yes	Eye-diagram suppression	
Two-band	Scalar	QAM	$I(t)\cos(\omega_c t) + Q(t)\sin(\omega_c t)$	I	$m_1(t) = \frac{\pi I(t)}{V_\pi}$	$J_0(m_2)J_0(m_1) + J_2(m_2)...$	Yes	Yes	Constellation compression + scaling	
		PSK	$V_s \sin[\omega_c t + \varphi_s(t)]$	PSK	$m_1 = \frac{\pi V_s}{V_\pi} = const.$	$J_0(m_1) \sin[\omega_c t + \varphi_s(t)]$	No	Small	No	
		OOK	$V_1(t)\sin(\omega_1 t) + V_2(t)\sin(\omega_2 t)$	OOK	$m_1(t) = \frac{\pi V_1(t)}{V_\pi}$ $m_2(t) = \frac{\pi V_2(t)}{V_\pi}$	$J_0(m_1)J_0(m_2) - 2J_2(m_2)J_2(m_1)...$	N/A	Yes	Eye-diagram suppression	
	Vector	QAM	$I_1(t)\cos(\omega_1 t) + Q_1(t)\sin(\omega_1 t) + I_2(t)\cos(\omega_2 t) + Q_2(t)\sin(\omega_2 t)$	I	$m_1(t) = \frac{\pi I_1(t)}{V_\pi}$	$[J_0(m_2)J_0(m_1) - 2J_2(m_2)J_2(m_1)]^2 + J_2(m_2)J_2(m_1)...$	Yes	Yes	Constellation compression + scaling	
		PSK	$V_1 \sin[\omega_1 t + \varphi_1(t)] + V_2 \sin[\omega_2 t + \varphi_2(t)]$	PSK	$m_1 = \frac{\pi V_1}{V_\pi} = const.$ $m_2 = \frac{\pi V_2}{V_\pi} = const.$	$J_0(m_2)J_0(m_1) \sin[\omega_1 t + \varphi_1(t)]$	No	Small	No	
		OOK	$V_1(t)\sin(\omega_1 t) + V_2(t)\sin(\omega_2 t)$	OOK	$m_1(t) = \frac{\pi V_1(t)}{V_\pi}$ $m_2(t) = \frac{\pi V_2(t)}{V_\pi}$	$J_0(m_1)J_0(m_2) \sin[\omega_1 t + \varphi_1(t)]$	No	Small	No	

- QAM signals suffer from both intra- and inter-band XM * **intra-band XM** * **inter-band XM**
- PSK signals has intrinsic resistance to intra-band I/Q XM and inter-band XM to other channels
- Scalar signals only suffer from inter-band XM
- All intra/inter-band XMs induce radical distortion to constellations, no phase rotation induced

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Outline



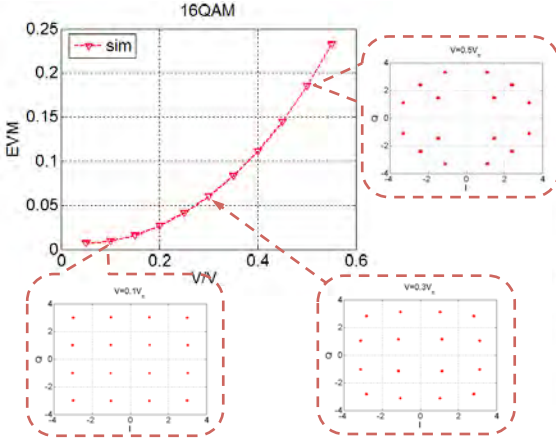
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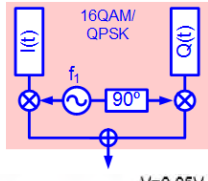
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Intra-band I/Q XM: 16QAM

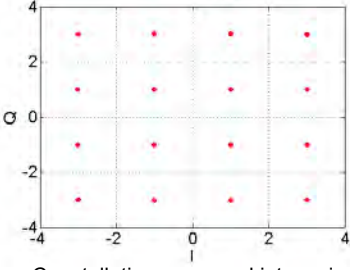


- Theoretical results





- Single-band vector signal




- Constellation squeezed into a circle

- $V \uparrow \rightarrow$ I/Q cross-modulation $\uparrow \rightarrow$ constellation distortion $\uparrow \rightarrow$ EVM \uparrow
- Outer points in constellation have larger I/Q amplitudes, also suffer more severe I/Q cross-modulation than inner points

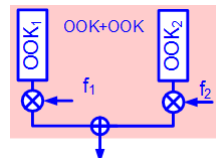
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Inter-band XM: OOK+OOK



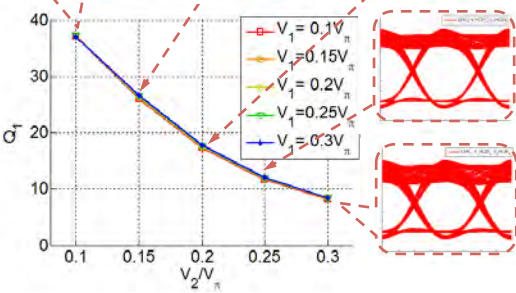
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- Theoretical results



OOK₁ OOK+OOK OOK₂
 f_1 f_2

- Two-band scalar signals



Q
 V_2/V_1


- $V_1 = 0.1V_\pi$
- $V_1 = 0.15V_\pi$
- $V_1 = 0.2V_\pi$
- $V_1 = 0.25V_\pi$
- $V_1 = 0.3V_\pi$

- Due to the lack of noise, Q_1 not dependent on V_1
- 5 curves for $0.1 < V_1/V_\pi < 0.3$ overlap

- As driving voltage of OOK₂ increases, $V_2 \uparrow$
 - Eye diagram of Ch1 degrades
 - Q-factor of OOK₁ reduces, $Q_1 \downarrow$

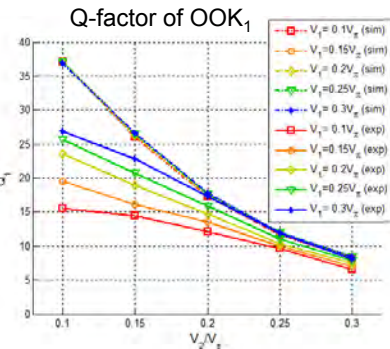
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Inter-band XM: OOK+OOK



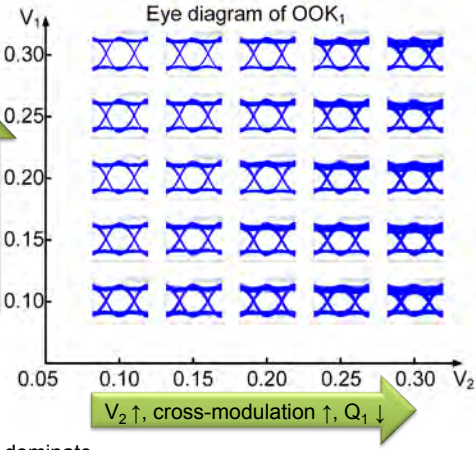
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- Experimental results



Q-factor of OOK₁
 Q_1
 V_2/V_1

- $V_1 = 0.1V_\pi$ (sim)
- $V_1 = 0.15V_\pi$ (sim)
- $V_1 = 0.2V_\pi$ (sim)
- $V_1 = 0.25V_\pi$ (sim)
- $V_1 = 0.3V_\pi$ (sim)
- $V_1 = 0.1V_\pi$ (exp)
- $V_1 = 0.15V_\pi$ (exp)
- $V_1 = 0.2V_\pi$ (exp)
- $V_1 = 0.25V_\pi$ (exp)
- $V_1 = 0.3V_\pi$ (exp)



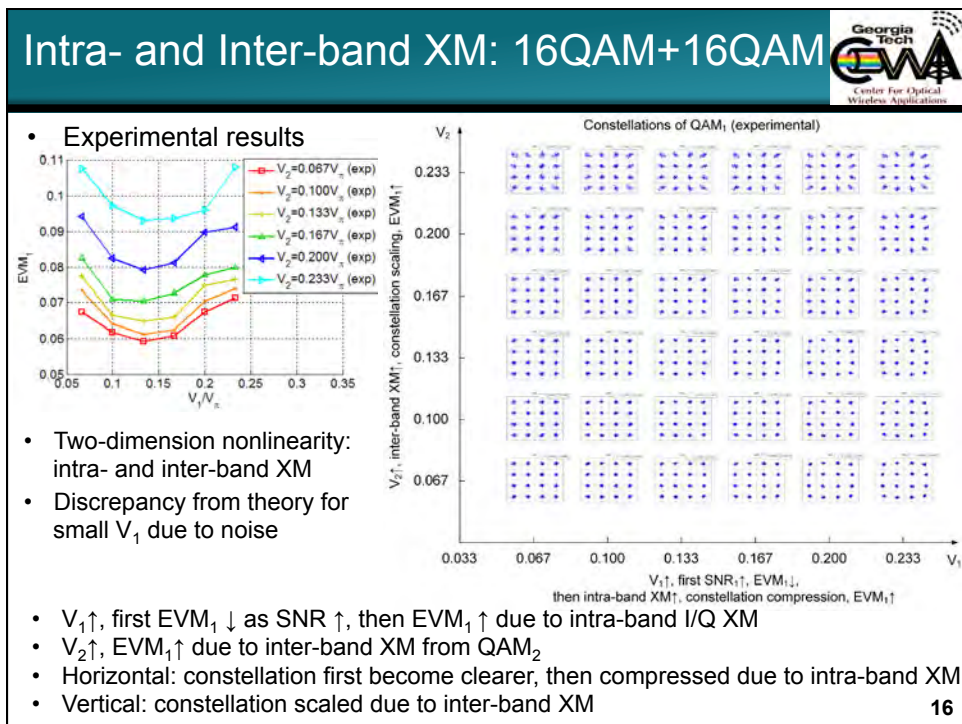
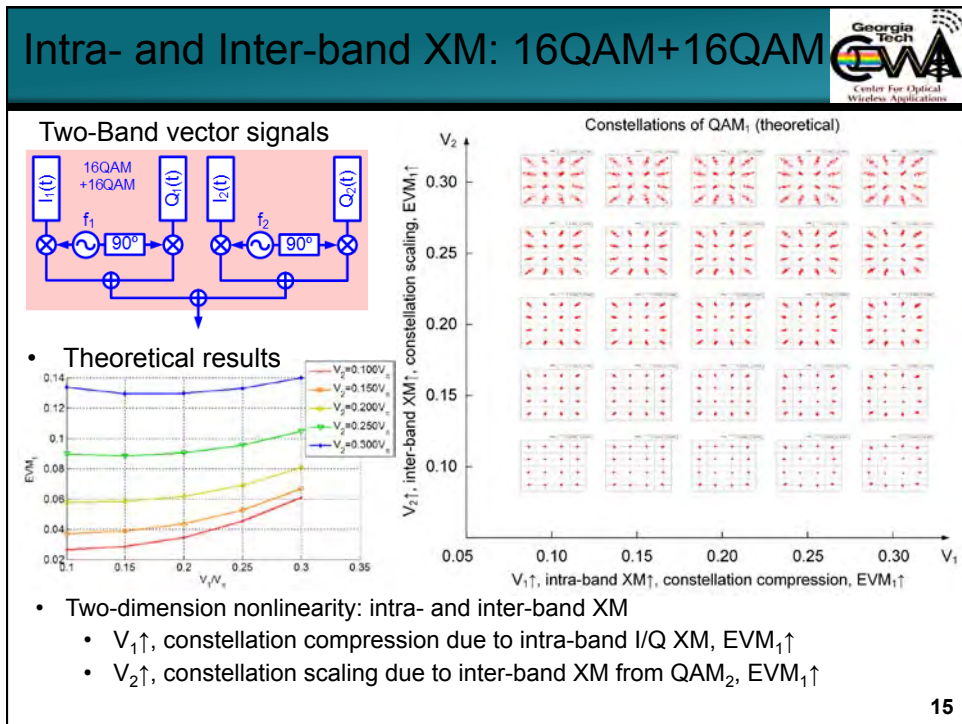
Eye diagram of OOK₁
 V_1
 V_2

$V_1 \uparrow, \text{SNR} \uparrow, Q_1 \uparrow$

$V_2 \uparrow, \text{cross-modulation} \uparrow, Q_1 \downarrow$

- Small V_2
 - Weak inter-band cross-modulation, noise dominate
 - Experimental Q_1 deviates from theoretical limit
- Large V_2
 - Cross-modulation dominate, experimental Q_1 approaches theoretical limit

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 - **Inter-band**

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Mitigate Intra-band XM


The diagram illustrates the experimental setup for mitigating intra-band cross-modulation (XM) in a 16QAM system. It shows a Central Office (CO) and a Remote Access Unit (RAU). The CO includes a CW Laser, a Dual-arm MZM with DC bias, and an Arcsine Pre-compensation block. The RAU includes an Amplifier, a Bandpass Filter (BPF), a Photodetector (PD), and a Sampling scope. The signal path is labeled with points A, B, C, and D. A graph shows the Error Vector Magnitude (EVM) versus the normalized voltage V/V_c for 16QAM, comparing simulation (sim) and experimental (exp) results. The graph shows that EVM increases significantly as V/V_c increases, and that pre-compensation (point D) significantly reduces EVM compared to no pre-compensation (point B).

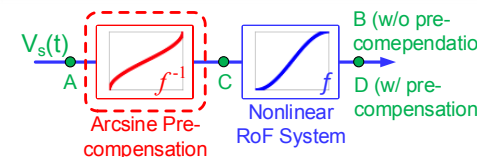
Point	Configuration	EVM
A	Original QAM	3.79%
B	QAM, w/o pre-compensation, $V_c=0.3784V_c$	12.41%
C	QAM, after pre-compensation	7.54%
D	QAM, w/ pre-compensation, $V_c=0.4476V_c$	5.07%

- **B**: 16QAM suffers from intra-band I/Q XM, constellation compression
- **C**: arcsine pre-compensation stretches the constellation
- **D**: constellation compression effect is canceled
- EVM reduced to ~5%, approaching noise limit

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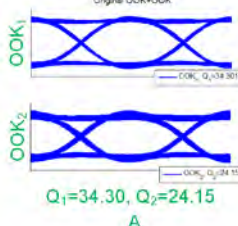
Mitigate Inter-band XM





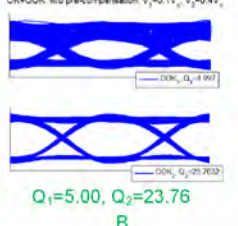
- Cancel inter-band between two OOK signals

Original OOK



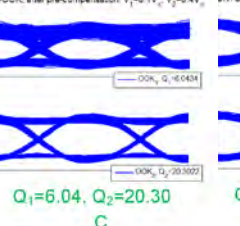
A
 $Q_1=34.30, Q_2=24.15$

OOK w/o pre-compensation $V_1=0.1V_{\pi}, V_2=0.4V_{\pi}$



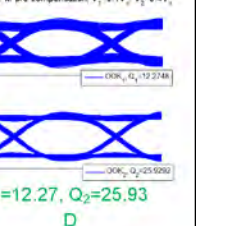
B
 $Q_1=5.00, Q_2=23.76$

OOK after pre-compensation $V_1=0.1V_{\pi}, V_2=0.4V_{\pi}$



C
 $Q_1=6.04, Q_2=20.30$

OOK w/ pre-compensation $V_1=0.1V_{\pi}, V_2=0.4V_{\pi}$




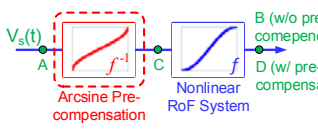
D
 $Q_1=12.27, Q_2=25.93$

- **A:** $V_1=0.1V_{\pi}, V_2=0.4V_{\pi}$
- **B:** Eye opening of OOK₁ suppressed by inter-band XM from OOK₂, $Q_1=4.997$
- **C:** Pre-compensation also induces XM ($Q_1=6.04$), but in an opposite way
- **D:** Inter-band XM canceled, and Q factors improved ($Q_1=12.27$)

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Mitigate Both Intra- and Inter-band XM





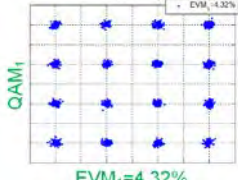
A: $V_1=0.25V_{\pi}, V_2=0.15V_{\pi}$

B: QAM₁ suffers from intra-band XM (constellation compression)
QAM₂ suffers from inter-band XM (constellation scaling)

C: Constellations stretched

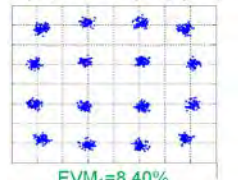
D: Pre-compensation cancels both intra- and inter-band XM

Original QAM₁ $EVM_1=4.32\%$



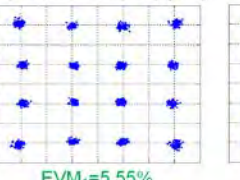
A
 $EVM_1=4.32\%$

QAM₁ w/o pre-compensation $V_1=0.25V_{\pi}, V_2=0.15V_{\pi}$



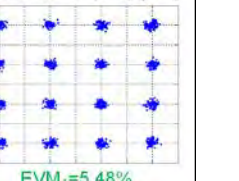
B
 $EVM_1=8.40\%$

QAM₁ after pre-compensation $V_1=0.25V_{\pi}, V_2=0.15V_{\pi}$



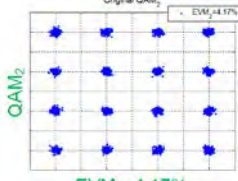
C
 $EVM_1=5.55\%$

QAM₁ w/ pre-compensation $V_1=0.25V_{\pi}, V_2=0.15V_{\pi}$



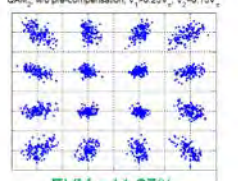
D
 $EVM_1=5.48\%$

Original QAM₂ $EVM_2=4.17\%$



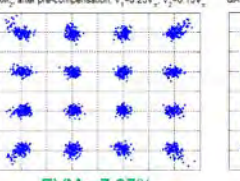
A
 $EVM_2=4.17\%$

QAM₂ w/o pre-compensation $V_1=0.25V_{\pi}, V_2=0.15V_{\pi}$



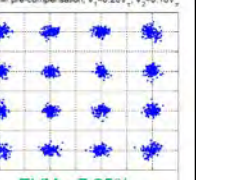
B
 $EVM_2=11.27\%$

QAM₂ after pre-compensation $V_1=0.25V_{\pi}, V_2=0.15V_{\pi}$




C
 $EVM_2=7.97\%$

QAM₂ w/ pre-compensation $V_1=0.25V_{\pi}, V_2=0.15V_{\pi}$



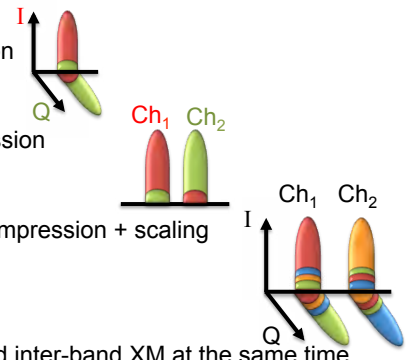
D
 $EVM_2=7.25\%$

Conclusions



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- Investigation of data channel XM in multi-band RoF system
 - Intra-band I/Q XM
 - 16QAM: constellation compression
 - Inter-band XM
 - OOK+OOK: eye diagram suppression
 - Both intra- and inter-band XM
 - 16QAM+16QAM: constellation compression + scaling
- Nonlinearity mitigation technique
 - Arcsine pre-compensation
 - Capable to compensate both intra- and inter-band XM at the same time
- Future research plan
 - Investigate the data pattern XM to OFDM
 - Consider both data XM and subcarrier IM



Diagrams illustrating I/Q axes and channel labels (Ch₁, Ch₂) for the investigated systems.

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Thank You!

Q & A



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